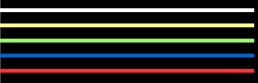


# Preemptive Detection of Unsafe Motion Liable for Hazard

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## High-level concerns

### What is safety?

- How infrequently a bad consequence could occur.

### Developer's concern

- How to support a safety claim  $<1$  crash/1mil.[km] in a quantifiable way?

### Regulator's concern

- Is the vehicle formally verifiable, certifiable and incrementally improved?
- How to find a technical defect at pre-market stage or after accumulation of accidents?

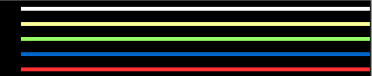
### Insurer's concern

- How to determine who is liable? Based on what legal scheme? What is legally valid evidence?

**Table 1. Examples of Miles and Years Needed to Demonstrate Autonomous Vehicle Reliability**

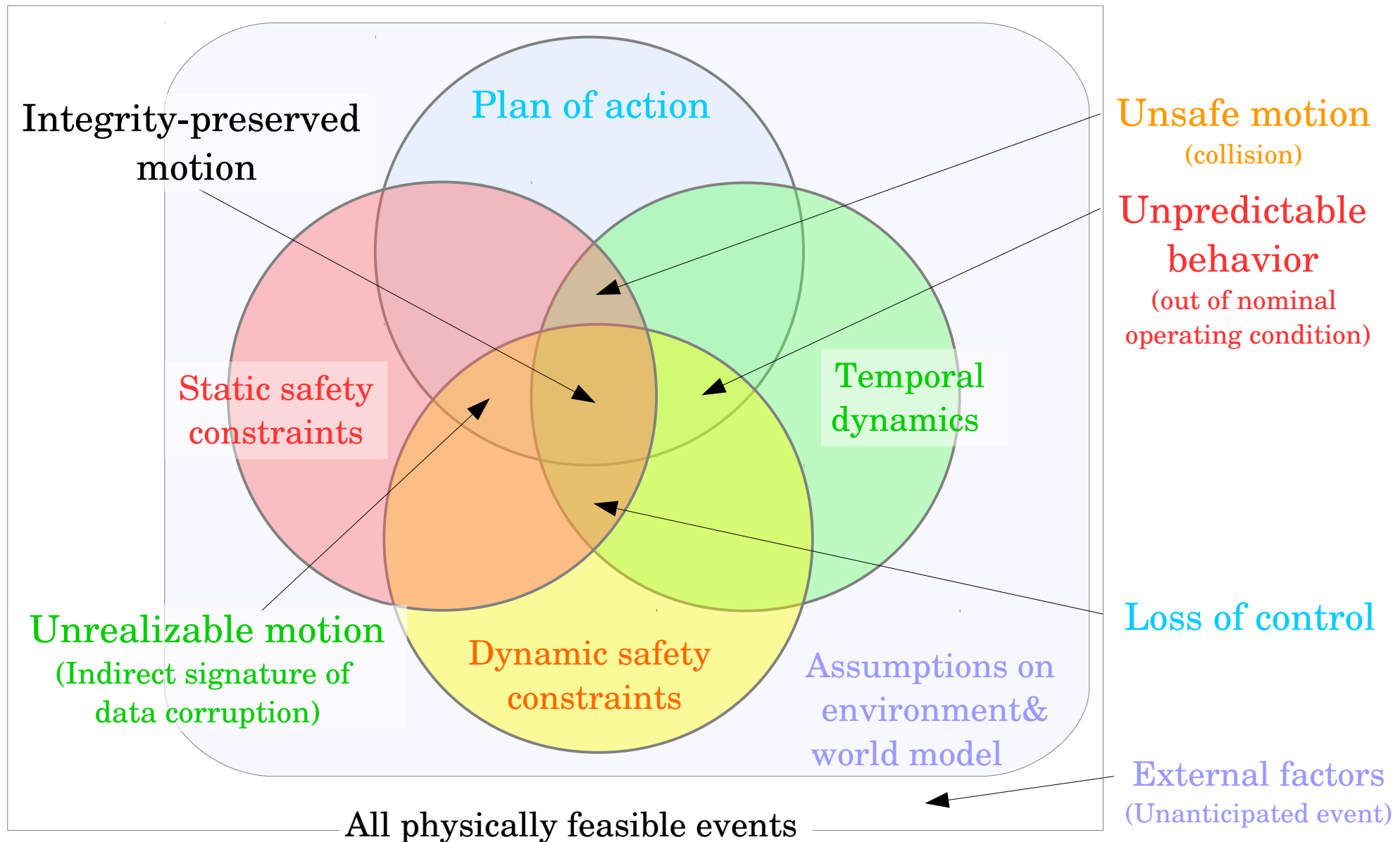
		Benchmark Failure Rate		
Statistical Question	How many miles (years <sup>a</sup> ) would autonomous vehicles have to be driven...	(A) 1.09 fatalities per 100 million miles?	(B) 77 reported injuries per 100 million miles?	(C) 190 reported crashes per 100 million miles?
	(1) without failure to demonstrate with 95% confidence that their failure rate is at most...	275 million miles (12.5 years)	3.9 million miles (2 months)	1.6 million miles (1 month)
	(2) to demonstrate with 95% confidence their failure rate to within 20% of the true rate of...	8.8 billion miles (400 years)	125 million miles (5.7 years)	51 million miles (2.3 years)
	(3) to demonstrate with 95% confidence and 80% power that their failure rate is 20% better than the human driver failure rate of...	11 billion miles (500 years)	161 million miles (7.3 years)	65 million miles (3 years)

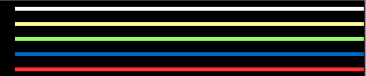
N. Kalra, S. M. Paddock, "How Many Miles of Driving Would It Take to Demonstrate Autonomous Vehicle Reliability?".RR1478, RAND Corporation



# Built-in defects: Loss of functional integrity

Direction 1: Detect loss of functional integrity by checking SATisfiability of these at run-time





# Externality of the risk of hazard

Direction 2: Determine liability based on a root-cause of evidently bad consequence

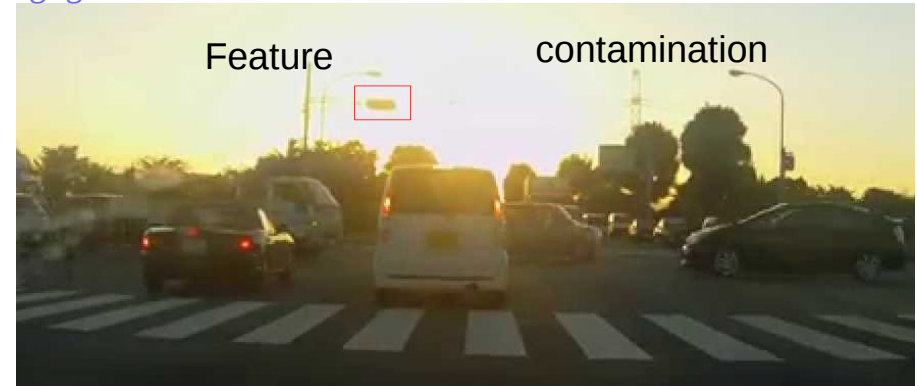
Plaintiff/Driver&Auto insurer:

“Unintended acceleration by itself!”

Defendant/OEM: “No evidence on record. You’re responsible for taking control as written in the disclaimer.”

Plaintiff/Regulator: “Recall all! Technical defect is repeatable!”

Defendant/OEM: “Reached the technological limit. Exempt from negligence claim.”



Plaintiff/Injured party: “My house got damaged!”

Defendant/Driver&Insurer: “Not my fault. The vehicle did it!”

Defect in the vehicle?

Root-cause built in the environment?

Plaintiff/Driver: “Go or brake?”

Defendant/Truck: “I turned, as you flashed.”

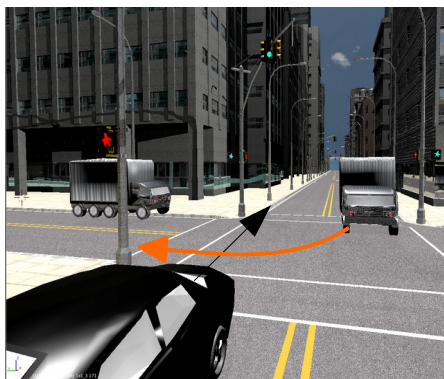
Plaintiff/OEM: “Repair it!”

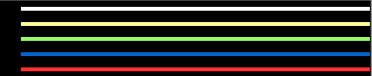
Defendant/Roadway Service: “Machine vision should keep attention. Just avoid it.”

Plaintiff/Driver,OEM&auto insurer:

“Lane departure due to poor lane marking”

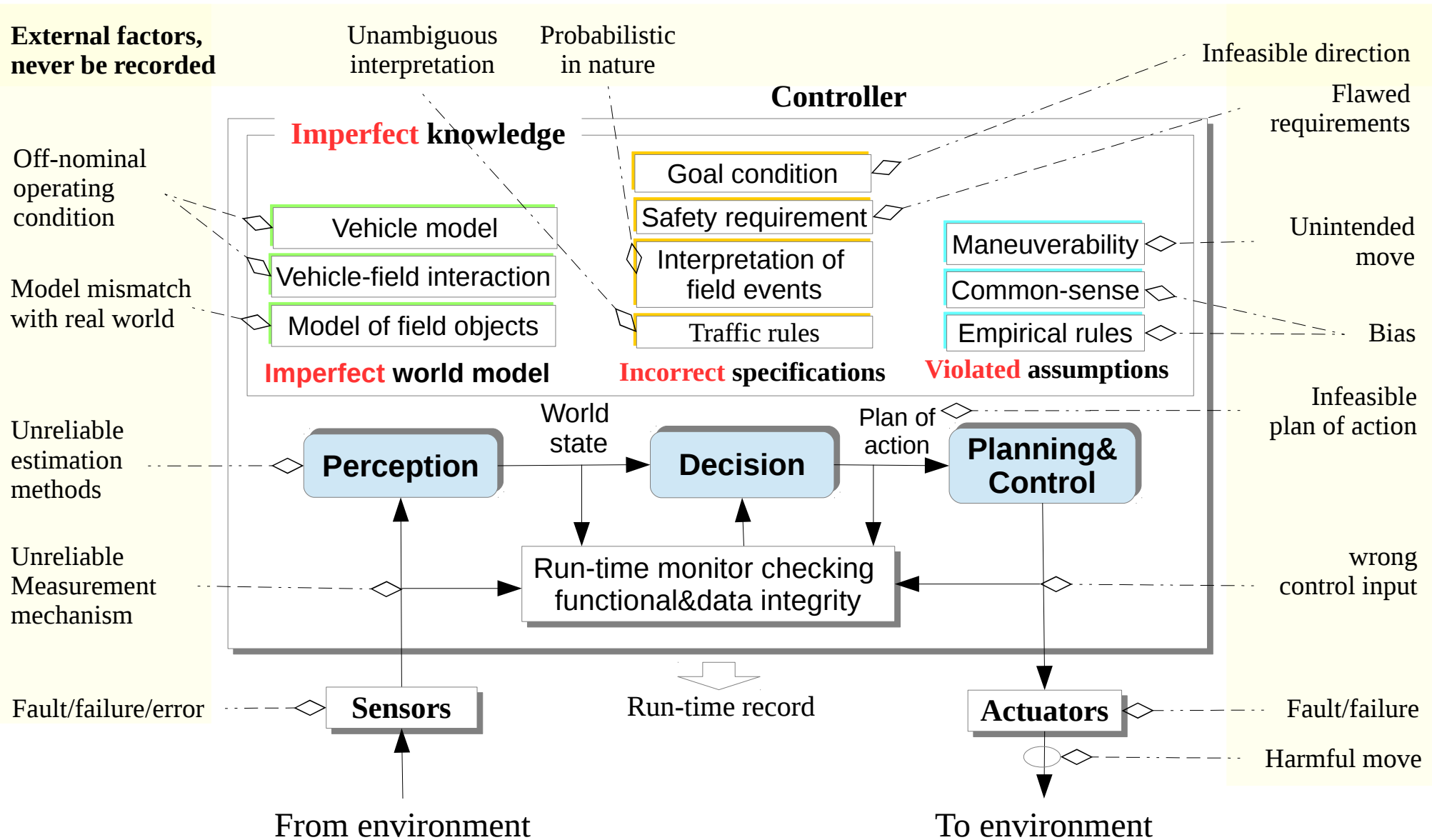
Defendant/Roadway Service: “We can guess effortlessly.”





# Single-points of failure: what if external factors=root-cause?

Direction3: Understand fundamental limits of determining liability based on root-cause analysis.  
 Formal root-cause analysis by solving MAXSAT is difficult, if only partially observable.

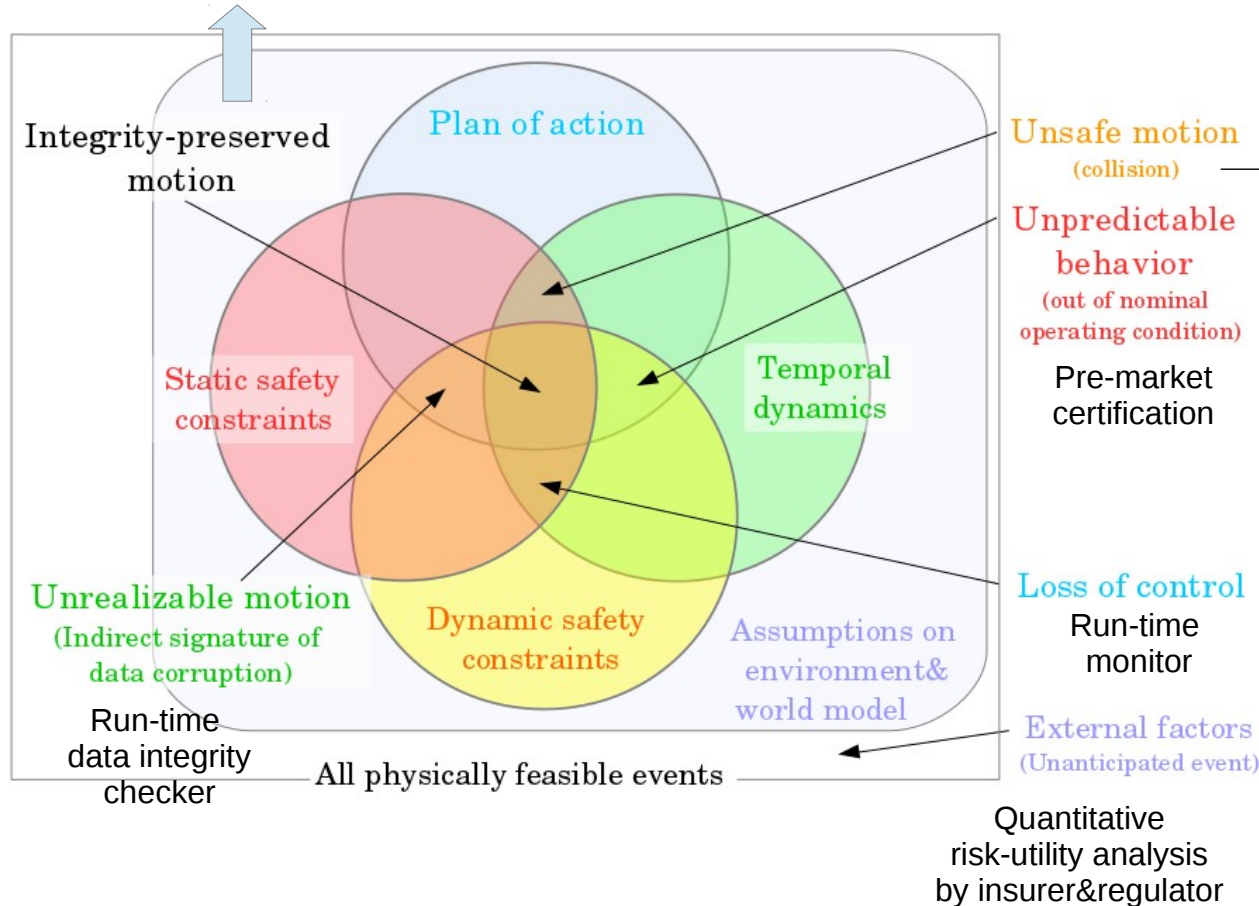




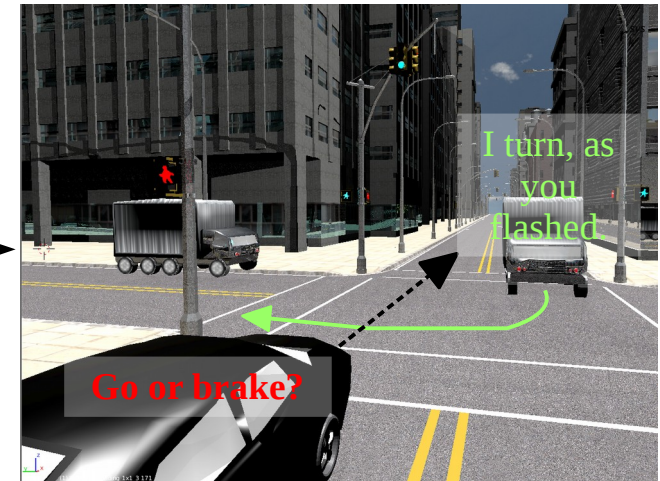
# What root-cause to detect preemptively? Non-stochastic?

Crash frequency becomes quantifiable, by preemptively detecting non-stochastic root-causes.

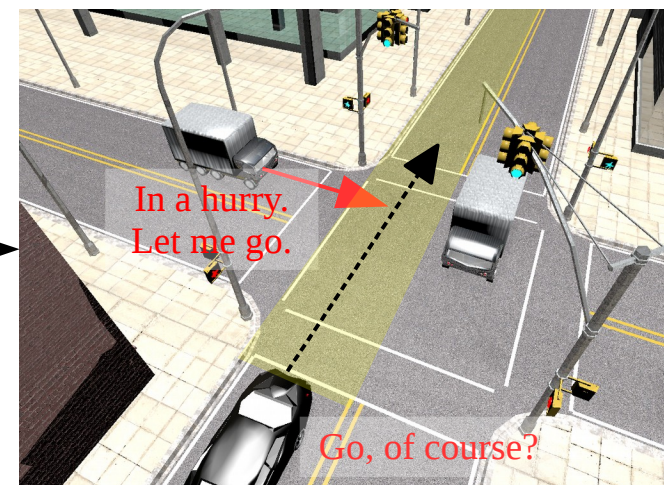
Report loss of functional integrity to the decision system

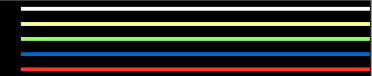


If you hit without evasive move...



or you don't have a right-of-way,





# Preemptive detection of infeasible plan of action/Loss-of-Control

## World state

$$\mathbf{X}_T \equiv \{\mathbf{x}_{0,\dots}, \mathbf{x}_T\}, \mathbf{U}_T \equiv \{\mathbf{u}_{0,\dots}, \mathbf{u}_T\}$$

$$0 \leq k < T, \mathbf{x}_k \equiv \{\vec{r}_k, v_k, \theta_k\} \in \mathbf{R}^4, \mathbf{u}_k \equiv \{a_k, \tau_k\} \in \mathbf{R}^2$$

{position, velocity, yaw angle}      {acceleration, yaw rate}

## Temporal dynamics

$$\mathbf{F}^{\text{sys}}(\mathbf{X}_T, \mathbf{U}_T) \equiv \begin{cases} -\vec{r}_{k+1} + \vec{r}_k + v_{k+1} \begin{bmatrix} \cos(\theta_{k+1}) \\ \sin(\theta_{k+1}) \end{bmatrix} \Delta t = \vec{0}, 0 \leq \forall k \leq T \\ -\begin{bmatrix} v_{k+1} \\ \theta_{k+1} \end{bmatrix} + \begin{bmatrix} v_k \\ \theta_k \end{bmatrix} + \begin{bmatrix} a_{k+1} \\ \tau_{k+1} \end{bmatrix} \Delta t = \vec{0}, 0 \leq \forall k \leq T \end{cases}$$

## Static safety constraint

$$\mathbf{S}^{\text{sys}}(\mathbf{X}_T, \mathbf{U}_T) \equiv \begin{bmatrix} \mathbf{u} \\ \mathbf{v} \end{bmatrix} \leq \begin{bmatrix} \mathbf{u}_k \\ \mathbf{v}_k \end{bmatrix} \leq \begin{bmatrix} \bar{\mathbf{u}} \\ \bar{\mathbf{v}} \end{bmatrix} \wedge \frac{d\mathbf{u}}{dt} \leq \frac{1}{\Delta t} (\mathbf{u}_{k+1} - \mathbf{u}_k) \leq \bar{d\mathbf{u}}$$

Mechanical limit of steering/acceleration

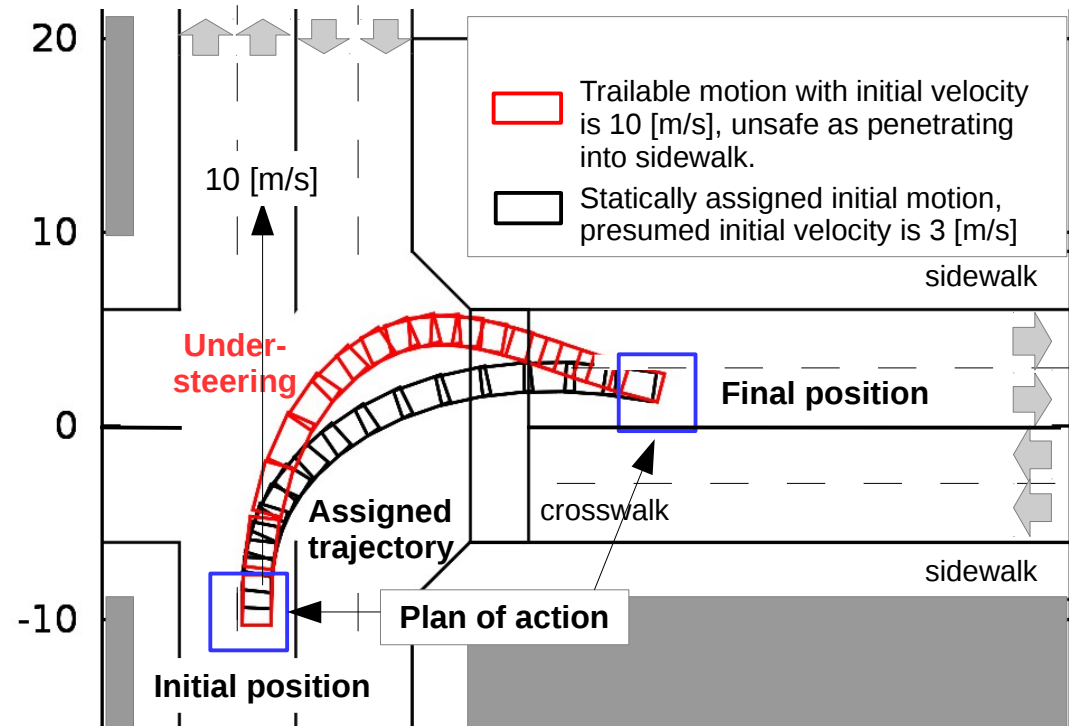
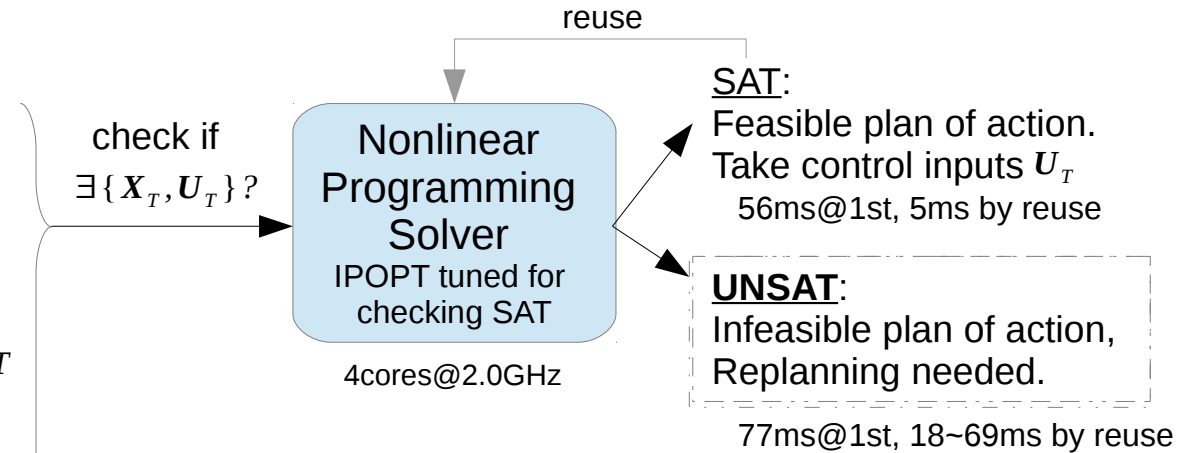
## Dynamic safety constraint

$$\mathbf{D}(\mathbf{X}_T) \equiv \{\vec{r}_k \in R_{\text{RIGHT-OF-WAY}} \mid 0 \leq \forall k \leq T\}$$

## Plan of action, route navigator demands to turn

$$\vec{r}_0 \in R_{\text{INIT}}, \vec{r}_T \in R_{\text{GOAL}}, \{\vec{r}_k \in R_{\text{REFERENCE\_PATH}} \mid 0 \leq \forall k \leq T\}$$

Terminal conditions      Simple path-following





# Preemptive detection of unsafe motion

by checking satisfiability of an adversarial motion planning from the mover's standpoint

## Plan of action

$$\vec{r}_0^{\text{sys}} \in R_{\text{INIT}}, \vec{r}_T^{\text{sys}} \in R_{\text{GOAL}}, \{ \vec{r}_k^{\text{sys}} \in R_{\text{REFERENCE\_PATH}} \mid 0 \leq \forall k \leq T \}$$

## World state

$$\mathbf{X}_{i,T}^{\text{mover}} \equiv \{ \mathbf{x}_{i,0}^{\text{mover}}, \dots, \mathbf{x}_{i,T}^{\text{mover}} \}, \mathbf{U}_{i,T}^{\text{mover}} \equiv \{ \mathbf{u}_{i,0}^{\text{mover}}, \dots, \mathbf{u}_{i,T}^{\text{mover}} \}$$

$$\mathbf{x}_{i,k}^{\text{mover}} := \{ \vec{r}_{i,k}, v_{i,k}, \theta_{i,k} \} \in \mathbf{R}^4, \mathbf{u}_{i,k}^{\text{mover}} \equiv \{ a_{i,k}, \tau_{i,k} \} \in \mathbf{R}^2$$

{position, velocity, yaw angle}    {acceleration, yaw rate}

## Temporal dynamics

$$\mathbf{F}^{\text{mover}}(\mathbf{X}_{i,T}^{\text{mover}}, \mathbf{U}_{i,T}^{\text{mover}}) \equiv \begin{cases} -\vec{r}_{k+1} + \vec{r}_{i,k} + v_{i,k+1} \begin{bmatrix} \cos(\theta_{i,k+1}) \\ \sin(\theta_{i,k+1}) \end{bmatrix} \Delta t = \vec{0} \\ -\begin{bmatrix} v_{i,k+1} \\ \theta_{i,k+1} \end{bmatrix} + \begin{bmatrix} v_{i,k} \\ \theta_{i,k} \end{bmatrix} + \begin{bmatrix} a_{i,k+1} \\ \tau_{i,k+1} \end{bmatrix} \Delta t = \vec{0} \end{cases}$$

## Assumption on maneuverability of mover

$$\mathbf{S}^{\text{mover}}(\mathbf{X}_{i,T}^{\text{mover}}, \mathbf{U}_{i,T}^{\text{mover}}) \equiv \begin{bmatrix} \underline{u}_i \\ \underline{v}_i \end{bmatrix} \leq \begin{bmatrix} \mathbf{u}_{i,k} \\ \mathbf{v}_{i,k} \end{bmatrix} \leq \begin{bmatrix} \bar{u}_i \\ \bar{v}_i \end{bmatrix} \wedge$$

Physical limit of rotation/acceleration

$$\frac{d\mathbf{u}_i}{dt} \leq \frac{1}{\Delta t} (\mathbf{u}_{i,k+1} - \mathbf{u}_{i,k}) \leq \bar{d\mathbf{u}_i}$$

Smoothness of the mover's motion

## Dynamic safety constraint

$$\mathbf{D}(\mathbf{X}_T^{\text{sys}}, \mathbf{X}_{i,T}^{\text{mover}}) \equiv \neg \bigvee_{0 \leq k \leq T} \text{haz}(\vec{r}_k^{\text{sys}}, \vec{r}_{i,k})$$

check if

$$\exists \{ \mathbf{X}_{i,T}^{\text{mover}}, \mathbf{U}_{i,T}^{\text{mover}} \} ?$$

Nonlinear  
Programming  
Solver

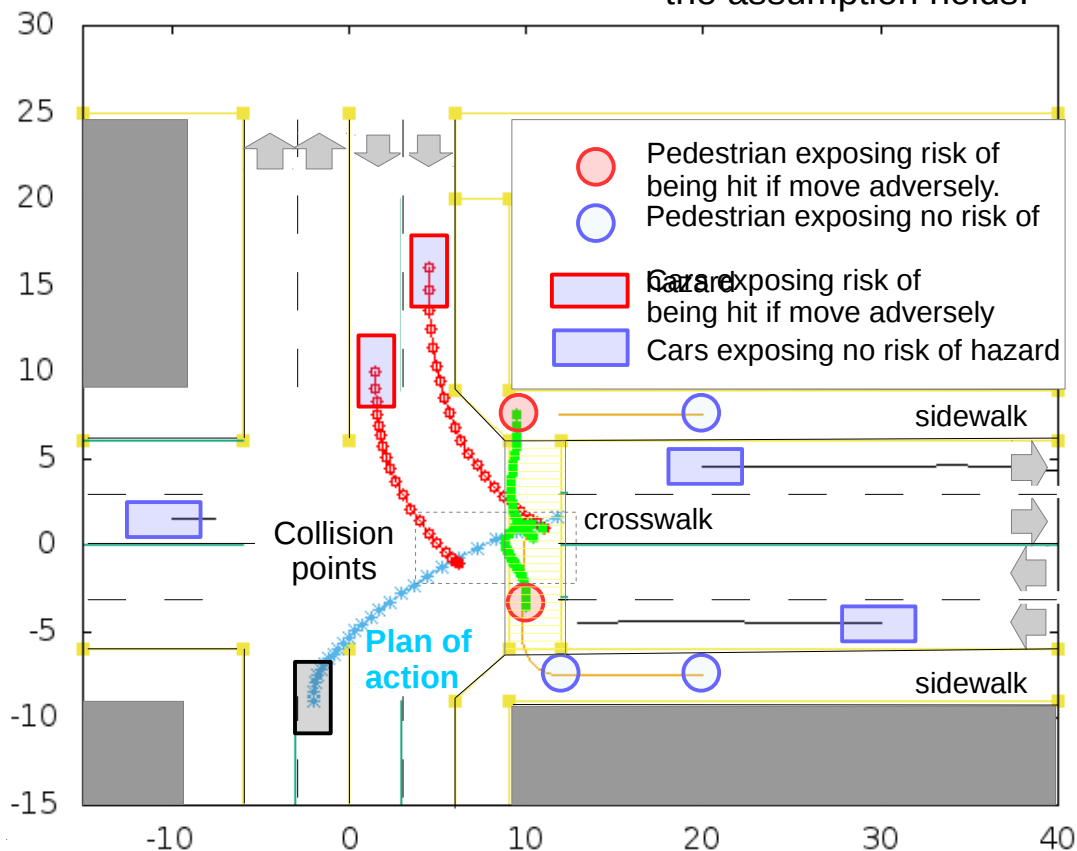
**SAT:**

Feasible adversarial move.  
Risk of hazard detected

10 movers at once in parallel  
71~89ms@1st, 28-59ms by reuse

**UNSAT:**

No risk of hazard **UNTIL**  
the assumption holds.



# Determining liability in a legal context

## Offense strategies

Payment for victims and owners of defective product

**(Strict) liability** : Unconditional compensation for damage from defects and failure of warning

**Negligence** : Protection of vehicle owner against conditioned design fault

- **Foresee** at least known risk of hazard

- **Act responsibly** to avoid the hazard

**Misrepresentation** : False/misleading information on functionality & the risk of hazard

**Breach of warranty** : Failure of providing the stated functionality when used in foreseeable ways.

## Defense strategies

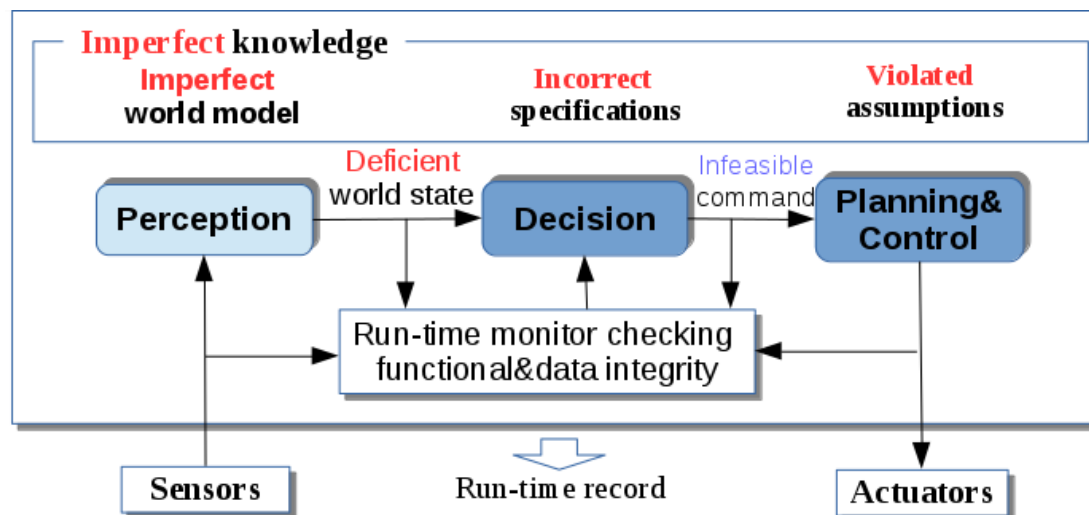
For waiver/reduction of OEM's liability

**Contributory negligence** : Insured party is partially liable, if **contributes to the hazard**.

**Consent/assumption of risk** : Signed **acknowledgment of the known&expressed risk** of hazard

**Necessity, limitation** : Exemption, if explicitly stated conditions hold.

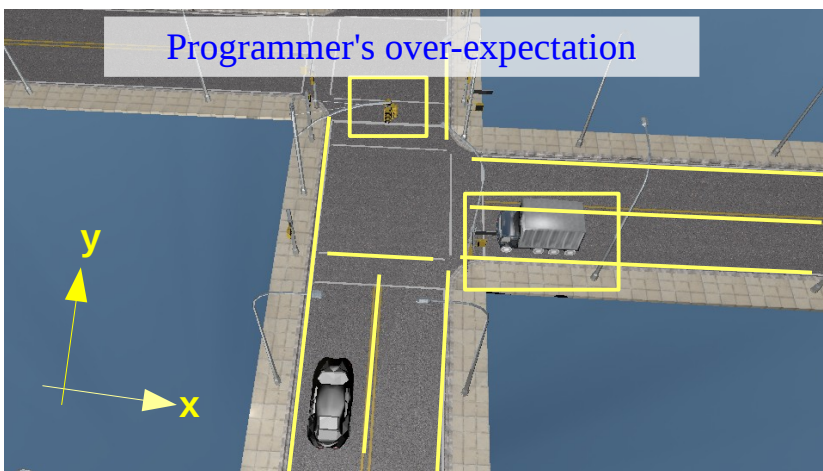
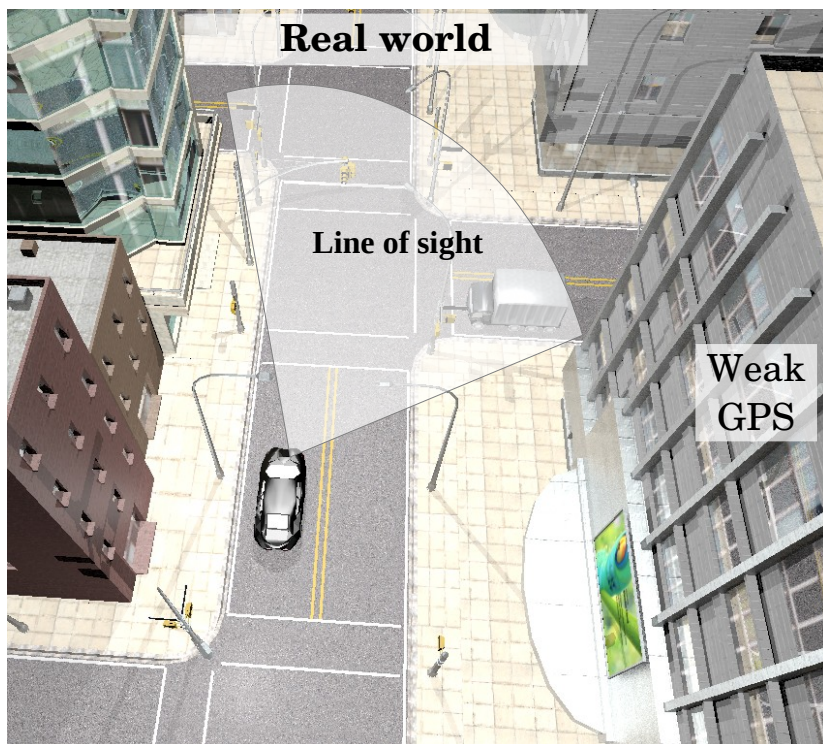
: Force Majeure clause, if **externality/unforeseeable/irresistibility** holds.



## Technical summary and implications

- Safety = How infrequently a bad consequence could occur.
- Liability = Each stakeholder's responsibility for predicting and avoiding the bad consequence.
- Proposals for determining liability and reducing crash frequency over time by design
  - Direction 1: Detect loss of functional integrity
    - Certification examiner must verify if the detection&recording function works.
  - Direction 2: Determine liability based on a root-cause of evidently bad consequence
  - Direction 3: Understand fundamental limits of determining liability based on the root-cause analysis.
    - Insurer should serve as a semi-independent auditor responsible for identifying a root-cause.
  - Direction 4: Determine liability using only observable states, based on contribution to hazard
    - If you hit without evasive move or without right-of-way, then you are at least partially liable.
- Detection mechanism
  - Detect loss of functional integrity event
  - Preemptive detection of infeasible plan of action, avoiding loss of control
  - Preemptive detection of unsafe motion, avoiding getting dynamic safety constraints violated.
    - Numerically check satisfiability using Nonlinear Programming solver

# Limited observability of world state



World state consists of

**Directly measurable part: Y**

Sensors produces, but sometimes get unavailable/unreliable.

**Unmeasurable part : X**

We can estimate it using a world model, if observable.

Time in 100 [ms]	0	1	2	..	50		
World state	Y[0]					error	Observable part
	...	Y: Directly measurable part					
	Y[10]				unavailable		
	X[0]						Unobservable part
	...	X: Unmeasurable part					
	X[100]				unknown		
	Z[0.100]	Not built in the world model					

